

FMRI Analysis

Experiment Design

Scanning

Pre-Processing

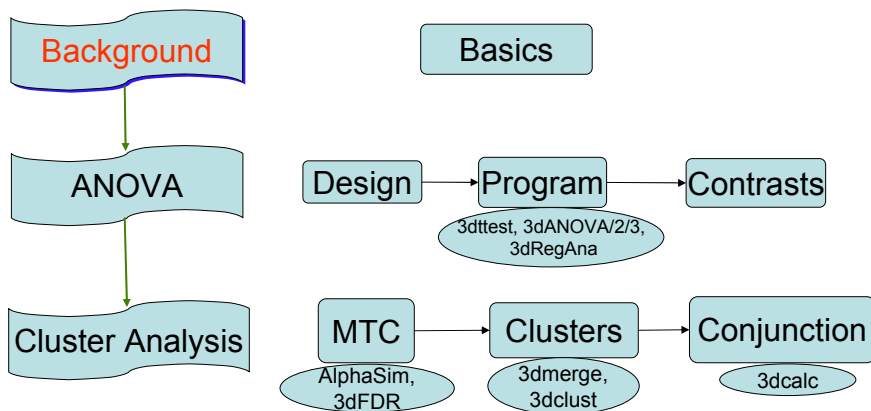
Individual Subject Analysis

Group Analysis

Post-Processing

-1-

Group Analysis



-2-

• Basics: Null hypothesis significance testing (NHST)

• Main function of statistics is to get more information into the data

• Null and alternative hypotheses

↳ H_0 : nothing happened vs. H_1 : something happened

• Dichotomous decision

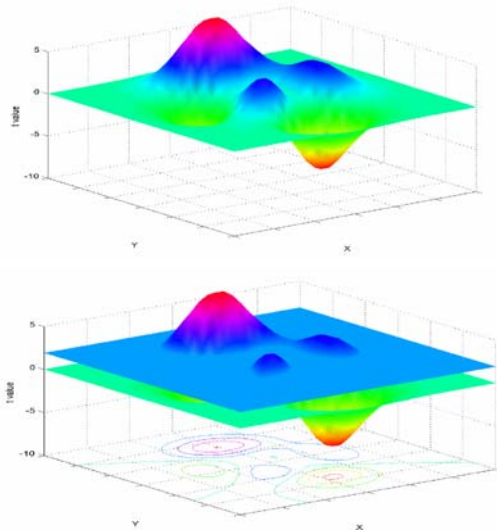
↳ Rejecting H_0 at a significant level α (e.g., 0.05)

↳ Subtle difference

Traditional: Hypothesis holds until counterexample occurs;

Statistical: discovery holds when a null hypothesis is rejected with some statistical confidence

↳ Topological landscape vs. binary world



-3-

• Basics: Null hypothesis significance testing (NHST)

• Dichotomous decision

↳ **Conditional probability** $P(\text{reject } H_0 \mid H_0) = \alpha \neq P(H_0)$!

↳ 2 types of errors and power

➢ Type I error = $\alpha = P(\text{reject } H_0 \mid H_0)$

➢ Type II error = $\beta = P(\text{accept } H_0 \mid H_1)$

➢ Power = $P(\text{accept } H_1 \mid H_1) = 1 - \beta$

Justice System: Trial

	Defendant Innocent	Defendant Guilty
Reject Presumption of Innocence (Guilty Verdict)	Type I Error	Correct
Fail to Reject Presumption of Innocence (Not Guilty Verdict)	Correct	Type II Error

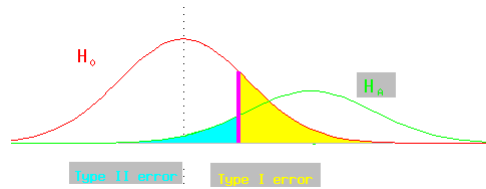
Statistics: Hypothesis Test

	H_0 True	H_0 False
Reject H_0	Type I Error	Correct
Fail to Reject H_0	Correct	Type II Error

-4-

• Basics: Null hypothesis significance testing (NHST)

↳ Compromise and strategy



- Lower type II error under fixed type I error
- Control false + while gaining as much power as possible
- Check **efficiency** (power) of design with **RSFgen** before scanning

↳ Typical misinterpretations^{*)}

- Reject $H_0 \rightarrow$ Prove or confirm a theory (alternative hypothesis)! (wrong!)
- $P(\text{reject } H_0 | H_0) = P(H_0)$ (wrong!)
- $P(\text{reject } H_0 | H_0) =$ Probability if the experiment can be reproduced (wrong!)

^{*)} Cohen, J., "The Earth Is Round ($p < .05$)" (1994), *American Psychologist*, 49, 12 997-1003

• Basics: Null hypothesis significance testing (NHST)

⌘ Controversy: Are humans cognitively good intuitive statisticians?

⌘ **Quiz:** HIV prevalence = 10^{-3} , false + of HIV test = 5%, power of HIV test ~ 100%.

↳ $P(\text{HIV+} | \text{test+}) = ?$

$$P(\text{HIV+} | \text{test+}) = \frac{P(\text{test+} | \text{HIV+})P(\text{HIV+})}{P(\text{test+} | \text{HIV+})P(\text{HIV+}) + P(\text{test+} | \text{HIV-})P(\text{HIV-})} = \frac{1.0 \times 10^{-3}}{1.0 \times 10^{-3} + 0.05 \times (1 - 10^{-3})} \approx 0.02$$

⌘ Keep in mind

- ↳ Better plan than sorry: Spend more time on experiment design (power analysis)
- ↳ More appropriate for detection than sanctification of a theory
 - Modern phrenology?
- ↳ Try to avoid unnecessary overstatement when making conclusions
- ↳ Present graphics and report % signal change, standard deviation, confidence interval, ...
- ↳ Replications are the best strategy on induction/generalization
 - Group analysis

Quiz

A researcher tested the null hypothesis that two population means are equal ($H_0: \mu_1 = \mu_2$). A t -test produced $p=0.01$. Assuming that all assumptions of the test have been satisfied, which of the following statements are true and which are false? Why?

1. There is a 1% chance of getting a result even more extreme than the observed one when H_0 is true.
2. There is a 1% likelihood that the result happened by chance.
3. There is a 1% chance that the null hypothesis is true.
4. There is a 1% chance that the decision to reject H_0 is wrong.
5. There is a 99% chance that the alternative hypothesis is true, given the observed data.
6. A small p value indicates a large effect.
7. Rejection of H_0 confirms the alternative hypothesis.
8. Failure to reject H_0 means that the two population means are probably equal.
9. Rejecting H_0 confirms the quality of the research design.
10. If H_0 is not rejected, the study is a failure.
11. If H_0 is rejected in Study 1 but not rejected in Study 2, there must be a moderator variable that accounts for the difference between the two studies.
12. There is a 99% chance that a replication study will produce significant results.
13. Assuming H_0 is true and the study is repeated many times, 1% of these results will be even more inconsistent with H_0 than the observed result.

Adapted from Kline, R. B. (2004). Beyond significance testing. Washington, DC: American Psychological Association (pp. 63-69). Dale Berger, CGU 9/04

Hint: Only 2 statements are true

-7-

Basics: Student's t

Background

- ↪ Gossett, 1908, Guinness brewing company, Dublin
- ↪ Named arbitrarily by R. A. Fisher
- ↪ Bell-shaped, but more spread out
- ↪ DF: asymptotically approaches $N(0,1)$ as $DF \rightarrow \infty$
- ↪ One tail or two?
- ↪ Special case of $F: F^2(n) = F(1, n)$

Usages: one-sample, two-sample, and paired t

One-sample

- Effect of a condition at group level
 - Group Mean relative to Standard Error of group Mean (SEM)
- $$T = \frac{\bar{X}_n - \mu}{S_n / \sqrt{n}} \quad S_n^2 = \frac{1}{n-1} \sum_{i=1}^n (X_i - \bar{X}_n)^2$$

Two-sample

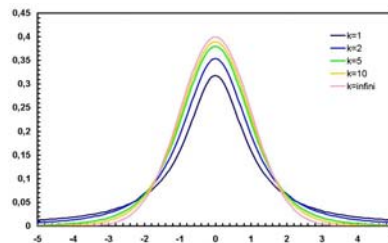
- Comparison between 2 groups
- (Difference of group means)/(Pooled SEM)

Paired

- Comparison between 2 conditions at group level
- (Difference of conditions)/(SEM of individual differences)
- ↪ Contrast and general linear test in regression and ANOVA
- 3dDeconvolve, 3dRegAna, 3dfim/+, 3dtttest, 3dANOVA/2/3

Assumptions

- ↪ Gaussian and Sphericity: heteroscedasticity in two-sample t



-8-

• Basics: F

¶ Background

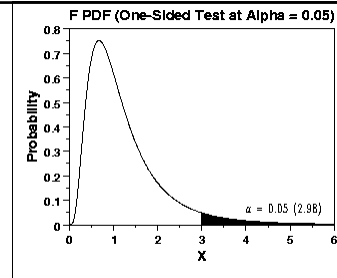
- ↳ Named after Sir R. A. Fisher
- ↳ Ratio of two Chi-square distributions
- ↳ Two parameters, $F(n_1, n_2)$
- ↳ One tail or two?
- ↳ t is a special case of F : $t^2(n) = F(1, n)$

¶ Usages:

- ↳ Two or more samples have the same variance?
 - ANOVA: Main effects and interactions
- ↳ What proportion of variation (effect) in the data is attributable to some cause?
 - Regression: Partial F and glt in **3dRegAna**, **3dDeconvolve**

¶ Assumptions

- ↳ Gaussian
- ↳ Sphericity
 - More than two conditions
 - Basis function modeling



-9-

• Basics: ANOVA

¶ Factor and level

- ↳ Dependant and independent variable
- ↳ Factors: categorizing variables, e.g., subject category and stimulus class
 - Subject categories: sex, genotypes, normal vs. patient
 - Stimulus categories: 4 (2x2) stimuli, object (human vs. tool), res (motion vs. points)
- ↳ Levels: nominal (qualitative) values of a factor
 - Object: human and tool; Resolution: high and low

¶ Fixed/random factor

- ↳ Fixed: specific levels of a factor are of interest
- ↳ Random (usually subject in fMRI)
 - Each level (a specific subject) of the factor is not of interest
 - But factor variance should be accounted for (cross-subject variation)
 - Random-effect model

¶ Different terminology for Factorial (crossed)/nested

- ↳ Count subject as a random factor (statisticians); Random-effect model
- ↳ Within-subject (repeated measures) / between-subjects (psychologists)
- ↳ Crossed and nested designs

¶ Group analysis

- ↳ Make general conclusions about some population
- ↳ Partition/untangle data variability into various sources (effect → causes)

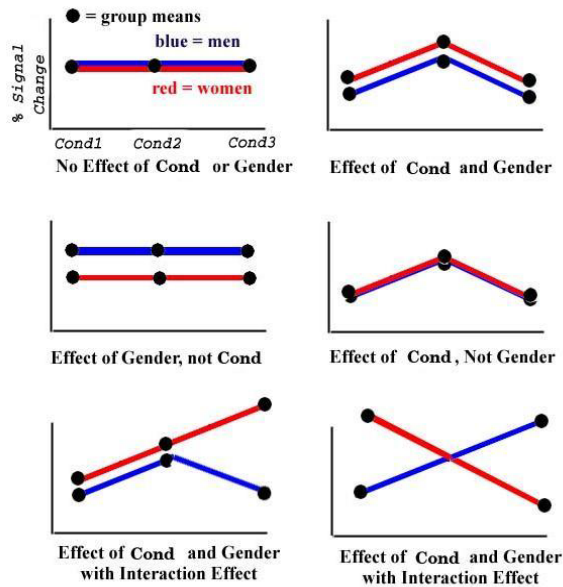
-10-

• Basics: ANOVA

More terminology

- **Main effect:**
general info regarding all levels of a factor
- **Simple effect:**
specific info regarding a factor level
- **Interaction:**
mutual/reciprocal influence among 2 or more factors; parallel or not?
- **Disordinal interaction:**
differences reverse sign
- **Ordinal interaction:**
one above another
- **Contrast:**
comparison of 2 or more simple effects; coefficients add up to 0
- **General linear test**

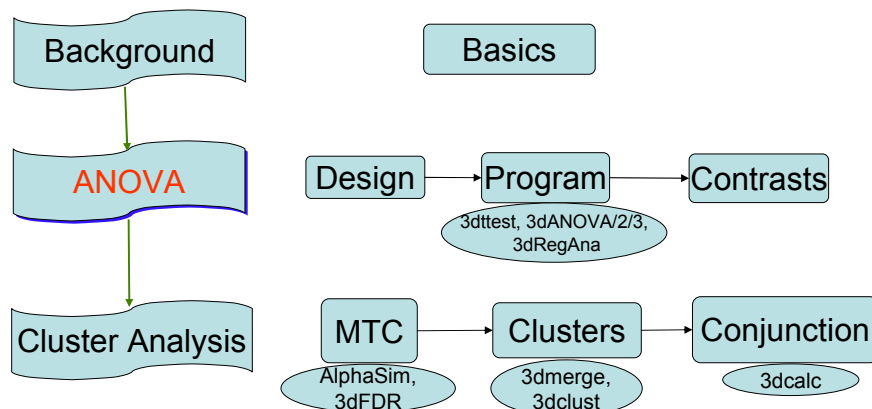
Main effects and Interactions Between Gender and Condition



Main effects and interactions in 2-way mixed ANOVA

-11-

Group Analysis



-12-

• Group Analysis: Overview

¶ Parametric Tests

- ↳ **3dttest** (one-sample, unpaired and paired t)
- ↳ **3dANOVA** (one-way between-subject)
- ↳ **3dANOVA2** (one-way within-subject, 2-way between-subjects)
- ↳ **3dANOVA3** (2-way between-subjects, within-subject and mixed, 3-way between-subjects)
- ↳ **3dRegAna** (regression/correlation, unbalanced ANOVA, ANCOVA)
- ↳ GroupAna (Matlab script for up to 5-way ANOVA)

¶ Non-Parametric Analysis

- ↳ No assumption of normality; Statistics based on ranking
- ↳ Appropriate when number of subjects too few
- ↳ Programs
 - **3dWilcoxon** (~ paired t -test)
 - **3dMannWhitney** (~ two-sample t -test)
 - **3dKruskalWallis** (~3dANOVA)
 - **3dFriedman** (~3dANOVA2)
 - Permutation test: plugin on AFNI under Define Datamode / Plugins /
- ↳ Can't handle complicated designs
- ↳ Less sensitive to outliers (more robust) and less flexible than parametric tests

-13-

• Group Analysis: Overview

¶ How many subjects?

- ↳ Power: proportional to \sqrt{n} ; $n > 10$
- ↳ Efficiency increases by the square root of # subjects
- ↳ Balance: Equal number of subjects across groups if possible

¶ Input

- ↳ % signal change (**not** statistics)
 - HRF magnitude: Regression coefficients
 - Contrast
- ↳ Common brain in tlrc space
 - Resolution: Doesn't have to be $1 \times 1 \times 1 \text{ mm}^3$

¶ Design

- ↳ Number of factors
- ↳ Number of levels for each factor
- ↳ Within-subject / repeated-measures vs. between-subjects
 - Fixed (factors of interest) vs. random (subject)
 - Nesting: Balanced?
- ↳ Which program?

¶ Contrasts

- ↳ One-tail or two-tail?

-14-

• Group Analysis : **3dtttest**

¶ Basic usage

↳ One-sample t

- One group: simple effect
- Example: 15 subjects under condition A with $H_0: \mu_A = 0$

↳ Two-sample t

- Two groups: Compare one group with another
- ~ 1-way between-subject (**3dANOVA2 -type 1**)
- Unequal sample sizes allowed
- Assumption of equal variance
- Example: 15 subjects under A and 13 other subjects under B - $H_0: \mu_A = \mu_B$

↳ Paired t

- Two conditions of one group: Compare one condition with another
- ~ one-way within-subject (**3dANOVA2 -type 3**)
- ~ one-sample t on individual contrasts
- Example: Difference between conditions A and B for 15 subjects with $H_0: \mu_A = \mu_B$

¶ Output: 2 values (% and t)

¶ Versatile program: Most tests can be done with **3dtttest**: piecemeal vs. bundled

-15-

• Group Analysis : **3dANOVA**

¶ Generalization of two-sample t -test

- ↳ One-way between-subject
- ↳ H_0 : no difference across all levels (groups)
- ↳ Examples of groups: gender, age, genotype, disease, *etc.*
- ↳ Unequal sample sizes allowed

¶ Assumptions

- ↳ Normally distributed with equal variances across groups

¶ Results: 2 values (% and t)

¶ **3dANOVA** vs. **3dtttest**

- ↳ Equivalent with 2 levels (groups)
- ↳ More than 2 levels (groups): Can run multiple two-sample t -test

-16-

• Group Analysis: 3dANOVA2

¶ Designs

↳ One-way within-subject (**type 3**)

- Major usage
- Compare conditions in one group
- Extension and equivalence of paired t

↳ Two-way between-subjects (**type 1**)

- 1 condition, 2 classifications of subjects
- Extension and equivalence two-sample t
- Unbalanced designs disallowed: Equal number of subjects across groups

¶ Output

↳ Main effect (**-fa**): F

↳ Interaction for two-way between-subjects (**-fab**): F

↳ Contrast testing

- Simple effect (**-amean**)
- 1st level (**-acontr**, **-adiff**): among factor levels
- 2nd level (interaction) for two-way between-subjects
- 2 values per contrast: % and t

-17-

• Group Analysis : 3dANOVA3

¶ Designs

↳ Three-way between-subjects (**type 1**)

- 3 categorizations of groups

↳ Two-way within-subject (**type 4**): Crossed design AXBXC

- Generalization of paired t -test
- One group of subjects
- Two categorizations of conditions: A and B

↳ Two-way mixed (**type 5**): Nested design BXC(A)

- Two or more groups of subjects (Factor A): subject classification, e.g., gender
- One category of condition (Factor B)
- Nesting: balanced

¶ Output

↳ Main effect (**-fa** and **-fb**) and interaction (**-fab**): F

↳ Contrast testing

- 1st level: **-amean**, **-adiff**, **-acontr**, **-bmean**, **-bdiff**, **-bcontr**
- 2nd level: **-abmean**, **-aBdiff**, **-aBcontr**, **-Abdiff**, **-Abcontr**
- 2 values per contrast : % and t

-18-

• Group Analysis: GroupAna

- ¶ Multi-way ANOVA
 - ↳ Matlab script package for up to 5-way ANOVA
 - ↳ Requires Matlab plus Statistics Toolbox
 - ↳ GLM approach (slow)
 - ↳ Powerful: Test for interactions
 - ↳ Downside
 - Difficult to test and interpret simple effects/contrasts
 - Complicated design, and compromised power
 - ↳ Heavy duty computation: minutes to hours
 - Input with lower resolution recommended
 - Resample with `adwarp -dxyz #` and `3dresample`
 - ↳ Can handle both volume and surface data
 - ↳ Can handle following unbalanced designs (two-sample *t* type):
 - 3-way ANOVA type 3: BXC(A)
 - 4-way ANOVA type 3: BXCXD(A)
 - 4-way ANOVA type 4: CXD(AXB)
- ¶ See <http://afni.nimh.nih.gov/sscc/gangc> for more info

-19-

• Group Analysis: Example

- ¶ Design
 - ↳ 4 conditions (TM, TP, HM, HP) and 8 subjects
 - ↳ 2-way within-subject: 2x2x8
 - A (Object), 2 levels: Tool vs Human
 - B (Animation), 2 levels: Motion vs Point
 - C (subject), 8 levels
 - AxBxC: Program?
- 3dANOVA3 -type 4**
- ¶ Main effects (A and B): 2 *F* values
- ¶ Interaction AXB: 1 *F*
- ¶ Contrasts
 - ↳ 1st order: TvsH, MvsP
 - ↳ 2nd order: TMvsTP, HMvsHP, TMvsHM, TPvsHP
 - ↳ 6x2 = 12 values
- ¶ Logistic
 - ↳ Input: 2x2x8 = 32 files (4 from each subject)
 - ↳ Output: 18 subbricks

-20-

• Group Analysis: Example

¶ Script

```
3dANOVA3 -type 4 -alevels 2 -blevels 2 -clevels 8 \
-dset 1 1 1 ED_TM_irf_mean+tlrc \
-dset 1 2 1 ED_TP_irf_mean+tlrc \
-dset 2 1 1 ED_HM_irf_mean+tlrc \
-dset 2 2 1 ED_HP_irf_mean+tlrc \
...
-adiff 1 2 TvsH1 \ (indices for difference)
-acontr 1 -1 TvsH2 \ (coefficients for contrast)
-bdiff 1 2 MvsP1 \
-aBdiff 1 2 : 1 TMvsHM \ (indices for difference)
-aBcontr 1 -1 : 1 TMvsHM \ (coefficients for contrast)
-aBcontr -1 1 : 2 HPvsTP \
-Abdiff 1 : 1 2 TMvsTP \
-Abcontr 2 : 1 -1 HMvsHP \

-fa ObjEffect \
-fb AnimEffect \
-fab ObjXAnim \

-bucket Group
```

Model type, number of levels for each factor

Input for each cell in ANOVA table: totally $2 \times 2 \times 8 = 32$

1st order Contrasts, paired *t* test

2nd order Contrasts, paired *t* test

Main effects & interaction *F* test; Equivalent to contrasts

Output: bundled

-21-

• Group Analysis: Example

¶ Alternative approaches

↳ GroupAna

↳ Paired *t*: 6 tests

➤ Program: 3dttest -paired

➤ For TM vs HM: 16 (2x8) input files (β coefficients: %) from each subject

```
3dttest -paired -prefix TMvsHM \
-set1 ED_TM_irf_mean+tlrc ... ZS_TM_irf_mean+tlrc \
-set2 ED_HM_irf_mean+tlrc ... ZS_HM_irf_mean+tlrc
```

↳ One-sample *t*: 6 tests

➤ Program: 3dttest

➤ For TM vs HM: 8 input files (contrasts: %) from each subject

```
3dttest -prefix TMvsHM \
-base1 0 \
-set2 ED_TMvsHM_irf_mean+tlrc ... ZS_TMvsHM_irf_mean+tlrc
```

-22-

• Group Analysis: ANCOVA

¶ Why ANCOVA?

- ↯ Subjects might not be an ideally randomized representation of a population
- ↯ If no controlled, cross-subject variability will lead to loss of power and accuracy
- ↯ Direct control: balanced selection of subjects
- ↯ Indirect (statistical) control: untangling covariate effect
- ↯ Covariate: uncontrollable and confounding variable, usually continuous
 - Age
 - Behavioral data, e.g., response time
 - Cortex thickness
 - Gender

¶ ANCOVA = Regression + ANOVA

- ↯ Assumption: linear relation between % signal change and the covariate
- ↯ GLM approach
- ↯ Avoid multi-way ANCOVA
 - Analyze partial data with one-way ANCOVA
 - Similar to running multiple one-sample or two-sample t test
- ↯ Centralize covariate so that it would not confound with other effects

-23-

• Group Analysis: ANCOVA Example

¶ Example: Running ANCOVA

- ↯ Two groups: 15 normal vs. 13 patients
- ↯ Analysis: comparing the two groups
- ↯ Running what test?
 - Two-sample t with 3dtttest
 - Controlling age effect?
- ↯ GLM model
 - $Y_i = \beta_0 + \beta_1 X_{1i} + \beta_2 X_{2i} + \beta_3 X_{3i} + \varepsilon_i, i = 1, 2, \dots, n (n = 28)$
 - Demean covariate (age) X_1
 - Code the factor (group) with a dummy variable
 - 0, when the subject is a patient;
 - $X_{2i} = \{$
 - 1, when the subject is normal.
 - With covariate X_1 centralized:
 - β_0 = effect of patient; β_1 = age effect (correlation coef); β_2 = effect of normal
 - $X_{3i} = X_{1i} X_{2i}$ models interaction (optional) between covariate and factor (group)
 - β_3 = interaction

-24-

• Group Analysis: ANCOVA Example

```
3dRegAna -rows 28 -cols 3 \
-
-workmem 1000 \
-
-xydata 0.1 0 0 patient/Pat1+tlrc.BRIK \
-xydata 7.1 0 0 patient/Pat2+tlrc.BRIK \
...
-xydata 7.1 0 0 patient/Pat13+tlrc.BRIK \
-xydata 2.1 1 2.1 normal/Norm1+tlrc.BRIK \
-xydata 2.1 1 2.1 normal/Norm2+tlrc.BRIK \
...
-xydata -8.9 1 -8.9 normal/Norm14+tlrc.BRIK \
-xydata 0.1 1 0.1 normal/Norm15+tlrc.BRIK \
-
-model 1 2 3 : 0 \
-
-bucket 0 Pat_vs_Norm \
-
-brick 0 coef 0 'Pat' \
-brick 1 tstat 0 'Pat t' \
-brick 2 coef 1 'Age Effect' \
-brick 3 tstat 1 'Age Effect t' \
-brick 4 coef 2 'Norm-Pat' \
-brick 5 tstat 2 'Norm-Pat t' \
-brick 6 coef 3 'Interaction' \
-brick 7 tstat 3 'Interaction t'
```

Model parameters: 28 subjects,
3 independent variables

Memory

Input: Covariates, factor levels,
interaction, and input files

Specify model for F and R²

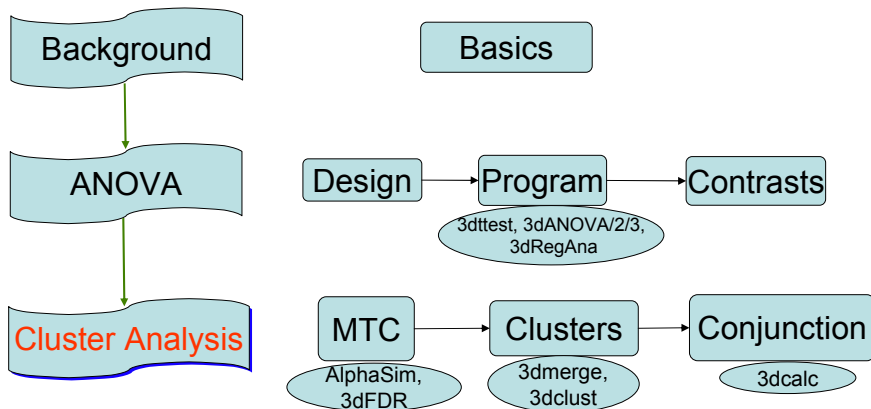
Output: #subbricks = 2*#coef + F + R²

Label output subbricks

See <http://afni.nimh.nih.gov/sscc/gangc/ANCOVA.html> for more information

-25-

Group Analysis



-26-

• Cluster Analysis: Multiple testing correction

- ¶ 2 types of errors in statistical tests
 - ↳ What is H_0 in FMRI studies?
 - ↳ Type I = $P(\text{reject } H_0 | \text{when } H_0 \text{ is true}) = \text{false positive} = p \text{ value}$
 - Type II = $P(\text{accept } H_0 | \text{when } H_1 \text{ is true}) = \text{false negative} = \beta$
 - ↳ Usual strategy: controlling type I error
 - (power = $1 - \beta$ = probability of detecting true activation)
 - ↳ Significance level = $\alpha: p < \alpha$
- ¶ Family-Wise Error (FWE)
 - ↳ Birth rate H_0 : sex ratio at birth = 1:1
 - What is the chance there are 5 boys (or girls) in a family?
 - Among 100 families with 5 kids, expected #families with 5 boys = ?
 - ↳ In fMRI H_0 : no activation at a voxel
 - What is the chance a voxel is mistakenly labeled as activated (false +)?
 - Multiple testing problem: With n voxels, what is the chance to mistakenly label at least one voxel? Family-Wise Error: $\alpha_{FW} = 1 - (1 - p)^n \rightarrow 1$ as n increases
 - Bonferroni correction: $\alpha_{FW} = 1 - (1 - p)^n \sim np$, if $p \ll 1/n$
 - Use $p = \alpha/n$ as individual voxel significance level to achieve $\alpha_{FW} = \alpha$

-27-

• Cluster Analysis: Multiple testing correction

- ¶ Multiple testing problem in fMRI: voxel-wise statistical analysis
 - ↳ Increase of chance at least one detection is wrong in cluster analysis
 - ↳ 3 occurrences of multiple testing: individual, group, and conjunction
 - ↳ Group analysis is the most concerned
- ¶ Two approaches
 - ↳ Control FWE: $\alpha_{FW} = P(\geq \text{one false positive voxel in the whole brain})$
 - Making α_{FW} small but without losing too much power
 - Bonferroni correction doesn't work: $p = 10^{-8} \sim 10^{-6}$
 - *Too stringent and overly conservative: Lose statistical power
 - Something to rescue? Correlation and structure!
 - *Voxels in the brain are not independent
 - *Structures in the brain
 - ↳ Control false discovery rate (FDR)
 - FDR = expected proportion of false + voxels among all detected voxels
 - ↳ Concrete example: individual voxel $p = 0.001$ for a brain of 25,000 EPI voxels
 - Uncorrected \rightarrow 25 false + voxels in the brain
 - FWE: corrected $p = 0.05 \rightarrow$ 1 false + among 20 brains for a fixed voxel location
 - FDR: corrected $p = 0.05 \rightarrow$ 5% voxels in those positively labeled ones are false +

-28-

• Cluster Analysis: AlphaSim

¶ FWE: Monte Carlo simulations

↳ Named for Monte Carlo, Monaco, where the primary attractions are casinos

↳ Program: **AlphaSim**

➢ Randomly generate some number (e.g., 1000) of brains with random noise

➢ Count the proportion of voxels are false + in all brains

➢ Parameters:

* ROI

* Spatial correlation

* Connectivity

* Individual voxel significant level (uncorrected p)

➢ Output

* Simulated (estimated) **overall significance level** (corrected p -value)

* Corresponding **minimum cluster size**

➢ Decision: Counterbalance among

* Uncorrected p

* Minimum cluster size

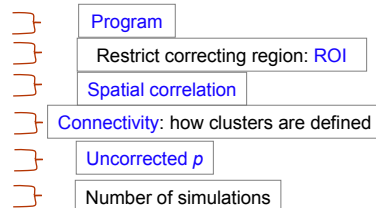
* Corrected p

-29-

• Cluster Analysis: AlphaSim

¶ Example

```
AlphaSim \
-mask MyMask+orig \
-fwhmx 4.5 -fwhmy 4.5 -fwhmz 6.5 \
-rmm 6.3 \
-pthr 0.0001 \
-iter 1000
```



¶ Output: 5 columns

↳ Focus on the 1st and last columns, and ignore others

↳ 1st column: minimum cluster size in voxels

↳ Last column: alpha (α), overall significance level (corrected p value)

Cl Size	Frequency	Cum Prop	p/Voxel	Max Freq	Alpha
2	1226	0.999152	0.00509459	831	0.859
3	25	0.998382	0.00015946	25	0.137
4	3	1.0	0.00002432	3	0.03

↳ May have to run several times with different uncorrected p : **uncorrected p ↔ cluster size**

-30-

• Cluster Analysis: 3dFDR

¶ Definition:

FDR = proportion of false + voxels among all detected voxels

$$FDR = \frac{N_{ai}}{D_a} = \frac{N_{ai}}{N_{ai} + N_{aa}}$$

¶ Doesn't consider

- ↳ spatial correlation
- ↳ cluster size
- ↳ connectivity

¶ Again, only controls the expected % false positives among declared active voxels

¶ Algorithm: statistic (t) → p value → FDR (q value) → z score

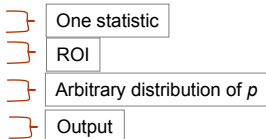
¶ Example:

3dFDR -input 'Group+tlrc[6]'

-mask_file mask+tlrc

-cdep -list

-output test



	Declared Inactive	Declared Active	
Truly Inactive	N_{ii}	$N_{ia} (I)$	T_i
Truly Active	$N_{ai} (II)$	N_{aa}	T_a
	D_i	D_a	

-31-

• Cluster Analysis: FWE or FDR?

¶ Correct type I error in different sense

↳ FWE: $\alpha_{FW} = P(\geq \text{one false positive voxel in the whole brain})$

- Frequentist's perspective: Probability among many hypothetical activation brains
- Used usually for parametric testing

↳ FDR = expected % false + voxels among all detected voxels

- Focus: controlling false + among detected voxels in one brain
- More frequently used in non-parametric testing

¶ Fail to survive correction?

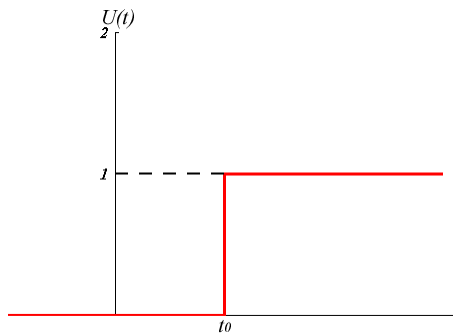
- ↳ At the mercy of reviewers
- ↳ Analysis on surface
- ↳ Tricks
 - One-tail?
 - ROI – cheating?
- ↳ Many factors along the pipeline
 - Experiment design: power?
 - Sensitivity vs specificity
 - Poor spatial alignment among subjects

-32-

• Cluster Analysis: Conjunction analysis

- ¶ Conjunction analysis
 - ↳ Common activation area
 - ↳ Exclusive activations
- ¶ Double/dual thresholding with AFNI GUI
 - ↳ Tricky
 - ↳ Only works for two contrasts
 - ↳ Common but not exclusive areas
- ¶ Conjunction analysis with `3dcalc`
 - ↳ Flexible and versatile
 - ↳ **Heaviside unit (step function)** defines a *On/Off* event

$$U(t-t_0) = \begin{cases} 1 & t \geq t_0 \\ 0 & t < t_0 \end{cases}$$



-33-

• Cluster Analysis: Conjunction analysis

- ¶ Example with 3 contrasts: A vs D, B vs D, and C vs D
 - ↳ Map 3 contrasts to 3 numbers: A > D: 1; B > D: 2; C > D: 4 (why 4?)
 - ↳ Create a mask with 3 subbricks of *t* (all with a threshold of 4.2)

```
3dcalc -a func+tlrc'[5]' -b func+tlrc'[10]' -c func+tlrc'[15]' \
-expr 'step(a-4.2)+2*step(b-4.2)+4*step(c-4.2)' \
-prefix ConjAna
```

- ↳ 8 ($=2^3$) scenarios:
 - 0: none;
 - 1: A > D but no others;
 - 2: B > D but no others;
 - 3: A > D and B > D but not C > D;
 - 4: C > D but no others;
 - 5: A > D and C > D but not B > D;
 - 6: B > D and C > D but not A > D;
 - 7: A > D, B > D and C > D

-34-

- **Miscellaneous**

- ⌘ Fixed-effects analysis
- ⌘ Sphericity and Heteroscedasticity
- ⌘ Trend analysis
- ⌘ Correlation analysis (aka functional connectivity)

-35-

- **Need Help?**

- ⚙ Command with “-help”
 - `3dANOVA3 -help`
- ⚙ Manuals
 - <http://afni.nimh.nih.gov/afni/doc/manual/>
- ⚙ Web
 - <http://afni.nimh.nih.gov/sscc/gangc>
- ⚙ Examples: HowTo#5
 - <http://afni.nimh.nih.gov/afni/doc/howto/>
- ⚙ Message board
 - <http://afni.nimh.nih.gov/afni/community/board/>
- ⚙ Appointment

➤ **Contact us @1-800-NIH-AFNI**

-36-